# **ANSWERS/HINTS**

#### **EXERCISE 1.1**

1. (i) 
$$2^2 \times 5 \times 7$$

(iv) 
$$5 \times 7 \times 11 \times 13$$

**2.** (i) LCM = 
$$182$$
; HCF =  $13$ 

3. (i) LCM = 
$$420$$
; HCF =  $3$ 

**4.** 22338

(ii) 
$$2^2 \times 3 \times 13$$

(v) 
$$17 \times 19 \times 23$$

$$LCM = 23460; HCF = 2$$

(iii) LCM = 3024; HCF = 6

(iii)  $3^2 \times 5^2 \times 17$ 

**7.** 36 minutes

# **EXERCISE 2.1**

(i) No zeroes

(ii) 1

(iii) 3

(iv) 2

(v) 4

(vi) 3

# **EXERCISE 2.2**

(iv) 
$$-2,0$$

2. (i) 
$$4x^2 - x - 4$$

(iv) 
$$x^2 - x + 1$$

(ii) 
$$\frac{1}{2}$$
,  $\frac{1}{2}$ 

(v) 
$$-\sqrt{15}$$
,  $\sqrt{15}$ 

(ii) 
$$3x^2 - 3\sqrt{2}x + 1$$

(v) 
$$4x^2 + x + 1$$

(iii) 
$$x^2 + \sqrt{5}$$

(vi) 
$$x^2 - 4x + 1$$

#### **EXERCISE 3.1**

1. (i) Required pair of linear equations is

x + y = 10; x - y = 4, where x is the number of girls and y is the number of boys.

To solve graphically draw the graphs of these equations on the same axes on graph paper.

Girls = 7, Boys = 3.

(ii) Required pair of linear equations is

5x + 7y = 50; 7x + 5y = 46, where x and y represent the cost (in  $\mathbb{T}$ ) of a pencil and of a pen respectively.

To solve graphically, draw the graphs of these equations on the same axes on graph paper.

Cost of one pencil = ₹ 3, Cost of one pen = ₹ 5

- 2. (i) Intersect at a point
- (ii) Coincident
- (iii) Parallel

3. (i) Consistent

- (ii) Inconsistent
- (iii) Consistent

(iv) Consistent

(v) Consistent

- 4. (i) Consistent
- (ii) Inconsistent
- (iii) Consistent
- (iv) Inconsistent

The solution of (i) above, is given by y = 5 - x, where x can take any value, i.e., there are infinitely many solutions.

The solution of (iii) above is x = 2, y = 2, i.e., unique solution.

- 5. Length = 20 m and breadth = 16 m.
- **6.** One possible answer for the three parts:
  - (i) 3x + 2y 7 = 0
- (ii) 2x + 3y 12 = 0
- (iii) 4x + 6y 16 = 0
- 7. Vertices of the triangle are (-1, 0), (4, 0) and (2, 3).

#### EXERCISE 3.3

1. (i) x = 9, y = 5

(ii) s = 9, t = 6

(iii) y = 3x - 3,

where x can take any value, i.e., infinitely many solutions.

(iv) x = 2, y = 3

(v) x = 0, y = 0

(vi) x = 2, y = 3

- **2.** x = -2, y = 5; m = -1
- 3. (i) x-y=26, x=3y, where x and y are two numbers (x>y); x=39, y=13.
  - (ii) x-y=18, x+y=180, where x and y are the measures of the two angles in degrees; x=99, y=81.
  - (iii) 7x + 6y = 3800, 3x + 5y = 1750, where x and y are the costs (in ₹) of one bat and one ball respectively; x = 500, y = 50.
  - (iv) x + 10y = 105, x + 15y = 155, where x is the fixed charge (in ₹) and y is the charge (in ₹ per km); x = 5, y = 10; ₹ 255.
  - (v) 11x-9y+4=0, 6x-5y+3=0, where x and y are numerator and denominator of the fraction;  $\frac{7}{9}$  (x = 7, y = 9).
  - (vi) x-3y-10=0, x-7y+30=0, where x and y are the ages in years of Jacob and his son; x=40, y=10.

#### **EXERCISE 3.3**

1. (i) 
$$x = \frac{19}{5}$$
,  $y = \frac{6}{5}$ 

(ii) 
$$x = 2$$
,  $y = 1$ 

(iii) 
$$x = \frac{9}{13}$$
,  $y = -\frac{5}{13}$ 

- (iv) x = 2, y = -3
- 2. (i) x-y+2=0, 2x-y-1=0, where x and y are the numerator and denominator of the fraction;  $\frac{3}{5}$ .
  - (ii) x-3y+10=0, x-2y-10=0, where x and y are the ages (in years) of Nuri and Sonu respectively. Age of Nuri (x) = 50, Age of Sonu (y) = 20.
  - (iii) x + y = 9, 8x y = 0, where x and y are respectively the tens and units digits of the number; 18.
  - (iv) x + 2y = 40, x + y = 25, where x and y are respectively the number of ₹ 50 and ₹ 100 notes; x = 10, y = 15.
  - (v) x + 4y = 27, x + 2y = 21, where x is the fixed charge (in ₹) and y is the additional charge (in ₹) per day; x = 15, y = 3.

# **EXERCISE 4.1**

- **1.** (i) Yes
- (ii) Yes
- (iii) No

(iv) Yes

- (v) Yes
- (vi) No
- (vii) No
- (viii) Yes
- 2. (i)  $2x^2 + x 528 = 0$ , where x is breadth (in metres) of the plot.
  - (ii)  $x^2 + x 306 = 0$ , where x is the smaller integer.
  - (iii)  $x^2 + 32x 273 = 0$ , where x (in years) is the present age of Rohan.
  - (iv)  $u^2 8u 1280 = 0$ , where u (in km/h) is the speed of the train.

### **EXERCISE 4.2**

1. (i) -2, 5

(ii)  $-2, \frac{3}{2}$ 

(iii) 
$$-\frac{5}{\sqrt{2}}, -\sqrt{2}$$

(iv)  $\frac{1}{4}, \frac{1}{4}$ 

(v)  $\frac{1}{10}$ ,  $\frac{1}{10}$ 

**2.** (i) 9,36

- (ii) 25,30
- 3. Numbers are 13 and 14.
- **4.** Positive integers are 13 and 14.

5. 5 cm and 12 cm

**6.** Number of articles = 6, Cost of each article = ₹ 15

#### **EXERCISE 4.3**

(i) Real roots do not exist (ii) Equal roots;  $\frac{2}{\sqrt{3}}$ ,  $\frac{2}{\sqrt{3}}$  (iii) Distinct roots;  $\frac{3 \pm \sqrt{3}}{2}$ 

- (i)  $k = \pm 2\sqrt{6}$
- (ii) k = 6
- 3. Yes. 40 m, 20 m

**4.** No

5. Yes. 20 m, 20 m

#### EXERCISE 5.1

(i) Yes. 15, 23, 31, ... forms an AP as each succeeding term is obtained by adding 8 in 1. its preceding term.

(ii) No. Volumes are V, 
$$\frac{3V}{4}$$
,  $\left(\frac{3}{4}\right)^2 V$ , ... (iii) Yes. 150, 200, 250, ... form an AP.

(iv) No. Amounts are 
$$10000 \left(1 + \frac{8}{100}\right)$$
,  $10000 \left(1 + \frac{8}{100}\right)^2$ ,  $10000 \left(1 + \frac{8}{100}\right)^3$ , ...

- 2. (i) 10, 20, 30, 40
- (iii) 4, 1, -2, -5

- (iv)  $-1, -\frac{1}{2}, 0, \frac{1}{2}$  (v) -1.25, -1.50, -1.75, -2.03. (i) a = 3, d = -2 (ii) a = -5, d = 4(iii)  $a = \frac{1}{3}, d = \frac{4}{3}$  (iv) a = 0.6, d = 1.1

(i) No

- (ii) Yes.  $d = \frac{1}{2}$ ; 4,  $\frac{9}{2}$ , 5
- (iii) Yes. d = -2; -9.2, -11.2, -13.2
- (iv) Yes. d = 4; 6, 10, 14
- (v) Yes.  $d = \sqrt{2}$ ;  $3 + 4\sqrt{2}$ ,  $3 + 5\sqrt{2}$ ,  $3 + 6\sqrt{2}$
- (vii) Yes. d = -4; -16, -20, -24
- (viii) Yes.  $d = 0; -\frac{1}{2}, -\frac{1}{2}, -\frac{1}{2}$

- (ix) No
- (x) Yes. d = a; 5a, 6a, 7a
- (xi) No
- (xii) Yes.  $d = \sqrt{2}$ ;  $\sqrt{50}$ ,  $\sqrt{72}$ ,  $\sqrt{98}$
- (xiii) No
- (xiv) No

(xv) Yes. d = 24; 97, 121, 145

## **EXERCISE 5.2**

- 1. (i)  $a_n = 28$  (ii) d = 2

- (iii) a = 46 (iv) n = 10 (v)  $a_n = 3.5$

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- **2.** (i) C
- (ii) B
- **3.** (i) 14
- (ii) 18,8
- (iii)  $\boxed{6\frac{1}{2}}, \boxed{8}$
- (iv)  $\begin{bmatrix} -2 \end{bmatrix}$ ,  $\begin{bmatrix} 0 \end{bmatrix}$ ,  $\begin{bmatrix} 2 \end{bmatrix}$ ,  $\begin{bmatrix} 4 \end{bmatrix}$
- (v) 53, 23, 8, -7

**4.** 16th term

- **5.** (i) 34
- (ii) 27

**6.** No

**7.** 178

**8.** 64

9. 5th term

**10.** 1

**11.** 65th term

**12.** 100

**13.** 128

**14.** 60

**15.** 13

- **16.** 4, 10, 16, 22, . . .
- 17. 20th term from the last term is 158.

(ii) -180

**18.** -13, -8, -3

**19.** 11th year

**20.** 10

# **EXERCISE 5.3**

- **1.** (i) 245
- (iii) 5505
- (iv)  $\frac{33}{20}$

**2.** (i)  $1046\frac{1}{2}$ 

(ii) 286

(iii) -8930

- 3. (i) n = 16,  $S_n = 440$
- (ii)  $d = \frac{7}{3}$ ,  $S_{13} = 273$
- (iii) a = 4,  $S_{12} = 246$

- (iv)  $d = -1, a_{10} = 8$
- (v)  $a = -\frac{35}{3}$ ,  $a_9 = \frac{85}{3}$
- (vi) n = 5,  $a_n = 34$

- (vii) n = 6,  $d = \frac{54}{5}$
- (viii) n = 7, a = -8
- (ix) d = 6

- (x) a = 4
- **4.** 12. By putting a = 9, d = 8, S = 636 in the formula  $S = \frac{n}{2}[2a + (n-1)d]$ , we get a quadratic equation  $4n^2 + 5n 636 = 0$ . On solving, we get  $n = -\frac{53}{4}$ , 12. Out of these two roots only one root 12 is admissible.
- 5. n = 16,  $d = \frac{8}{3}$
- **6.** n = 38, S = 6973
- 7. Sum = 1661

- **8.**  $S_{51} = 5610$
- **9.**  $n^2$

**10.** (i)  $S_{15} = 525$  (ii)  $S_{15} = -465$ 

- **11.**  $S_1 = 3, S_2 = 4; \ a_2 = S_2 S_1 = 1; \ S_3 = 3, \ a_3 = S_3 S_2 = -1, \ a_{10} = S_{10} S_9 = -15; \ a_n = S_n S_{n-1} = 5 2n.$
- **12.** 4920
- **13.** 960
- **14.** 625
- **15.** ₹ 27750
- **16.** Values of the prizes (in  $\overline{\epsilon}$ ) are 160, 140, 120, 100, 80, 60, 40.
- **17**. 234
- **18.** 143 cm
- 19. 16 rows, 5 logs are placed in the top row. By putting S = 200, a = 20, d = -1 in the formula  $S = \frac{n}{2}[2a + (n-1)d]$ , we get,  $41n n^2 = 400$ . On solving, n = 16, 25. Therefore, the number of rows is either 16 or 25.  $a_{25} = a + 24d = -4$

i.e., number of logs in 25th row is -4 which is not possible. Therefore n=25 is not possible. For n=16,  $a_{16}=5$ . Therefore, there are 16 rows and 5 logs placed in the top row.

**20.** 370 m

# **EXERCISE 5.4 (Optional)\***

- 1. 32nd term
- **2.**  $S_{16} = 20,76$
- 3. 385 cm

**4.** 35

5.  $750 \,\mathrm{m}^3$ 

# **EXERCISE 6.1**

1. (i) Similar

(ii) Similar

(iii) Equilateral

- (iv) Equal, Proportional
- **3.** No

#### **EXERCISE 6.2**

1. (i) 2 cm

(ii) 2.4 cm

**2.** (i) No

(ii) Yes

- (iiii) Yes
- 9. Through O, draw a line parallel to DC, intersecting AD and BC at E and F respectively.

#### **EXERCISE 6.3**

- 1. (i) Yes. AAA,  $\triangle$  ABC  $\sim$   $\triangle$  PQR
- (ii) Yes. SSS,  $\triangle$  ABC  $\sim$   $\triangle$  QRP

(iii) No

(iv) Yes. SAS,  $\Delta$  MNL  $\sim$   $\Delta$  QPR

(v) No

(vi) Yes. AA,  $\triangle$  DEF  $\sim \triangle$  PQR

- 2. 55°, 55°, 55°
- **14.** Produce AD to a point E such that AD = DE and produce PM to a point N such that PM = MN. Join EC and NR.
- **15.** 42 m

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#### EXERCISE 7.1

1. (i)  $2\sqrt{2}$ 

(ii)  $4\sqrt{2}$ 

(iii)  $2\sqrt{a^2+b^2}$ 

2. 39; 39 km

**3.** No

**4.** Yes

**5.** Champa is correct.

6. (i) Square

(ii) No quadrilateral

(iii) Parallelogram

7. (-7,0)

8. -9, 3

9.  $\pm 4$ . OR =  $\sqrt{41}$ . PR =  $\sqrt{82}$ .  $9\sqrt{2}$ 

**10.** 3x + y - 5 = 0

#### EXERCISE 7.2

**1.** (1, 3)

**2.**  $\left(2, -\frac{5}{3}\right)$ ;  $\left(0, -\frac{7}{3}\right)$ 

3.  $\sqrt{61}$  m; 5th line at a distance of 22.5 m

**5.** 1:1;  $\left(-\frac{3}{2}, 0\right)$  **6.** x = 6, y = 3

8.  $\left(-\frac{2}{7}, -\frac{20}{7}\right)$  9.  $\left(-1, \frac{7}{2}\right)$ , (0,5),  $\left(1, \frac{13}{2}\right)$ 

1. (i)  $\sin A = \frac{7}{25}$ ,  $\cos A = \frac{24}{25}$  (ii)  $\sin C = \frac{24}{25}$ ,  $\cos C = \frac{7}{25}$ 

3.  $\cos A = \frac{\sqrt{7}}{4}$ ,  $\tan A = \frac{3}{\sqrt{7}}$  4.  $\sin A = \frac{15}{17}$ ,  $\sec A = \frac{17}{8}$ 

5.  $\sin \theta = \frac{5}{13}$ ,  $\cos \theta = \frac{12}{13}$ ,  $\tan \theta = \frac{5}{12}$ ,  $\cot \theta = \frac{12}{5}$ ,  $\csc \theta = \frac{13}{5}$ 

(i)  $\frac{49}{64}$ 

(ii)  $\frac{49}{64}$ 

8. Yes

(i) 1

(ii) 0

10.  $\sin P = \frac{12}{13}$ ,  $\cos P = \frac{5}{13}$ ,  $\tan P = \frac{12}{5}$ 

(i) False 11.

(ii) True

(iii) False

(iv) False

(v) False

#### EXERCISE 8.2

1. (i) 1 (ii) 2 (iii) 
$$\frac{3\sqrt{2} - \sqrt{6}}{8}$$
 (iv)  $\frac{43 - 24\sqrt{3}}{11}$  (v)  $\frac{67}{12}$ 

**2.** (i) A (ii) D (iii) A (iv) C

3.  $\angle A = 45^{\circ}$ ,  $\angle B = 15^{\circ}$ 

**4.** (i) False (ii) True (iii) False

(iv) False (v) True

#### **EXERCISE 8.3**

1. 
$$\sin A = \frac{1}{\sqrt{1 + \cot^2 A}}, \tan A = \frac{1}{\cot A}, \sec A = \frac{\sqrt{1 + \cot^2 A}}{\cot A}$$

2. 
$$\sin A = \frac{\sqrt{\sec^2 A - 1}}{\sec A}$$
,  $\cos A = \frac{1}{\sec A}$ ,  $\tan A = \sqrt{\sec^2 A - 1}$ 

$$\cot A = \frac{1}{\sqrt{\sec^2 A - 1}}, \csc A = \frac{\sec A}{\sqrt{\sec^2 A - 1}}$$

# **3.** (i) B (ii) C (iii) D (iv) D **EXERCISE 9.1**

2. 
$$8\sqrt{3}$$
 m

5. 
$$40\sqrt{3}$$
 m

**6.** 
$$19\sqrt{3}$$
 m

1. 10 m 2.  $8\sqrt{3} \text{ m}$  3.  $3 \text{ m}, 2\sqrt{3} \text{ m}$  4.  $10\sqrt{3} \text{ m}$  5.  $40\sqrt{3} \text{ m}$  6.  $19\sqrt{3} \text{ m}$  7.  $20(\sqrt{3} - 1) \text{ m}$  8.  $0.8(\sqrt{3} + 1) \text{ m}$ 

9. 
$$16\frac{2}{3}$$
 m

9.  $16\frac{2}{3}$  m 10.  $20\sqrt{3}$  m, 20 m, 60 m 11.  $10\sqrt{3}$  m, 10 m 12.  $7(\sqrt{3}+1)$  m

13. 
$$75(\sqrt{3}-1)$$
m 14.  $58\sqrt{3}$  m

**15.** 3 seconds

#### **EXERCISE 10.1**

1. Infinitely many

2. (i) One (ii) Secant (iii) Two (iv) Point of contact

**3.** D

#### **EXERCISE 10.2**

**1.** A

**2.** B

**6.** 3 cm

7. 8 cm 12. AB = 15 cm, AC = 13 cm

#### **EXERCISE 11.1**

1.  $\frac{132}{7}$  cm<sup>2</sup> 2.  $\frac{77}{8}$  cm<sup>2</sup>

3.  $\frac{154}{3}$  cm<sup>2</sup>

(i)  $28.5 \, \text{cm}^2$ 

(ii) 235.5 cm<sup>2</sup>

(i) 22 cm

(ii) 231 cm<sup>2</sup>

(iii)  $\left(231 - \frac{441\sqrt{3}}{4}\right) \text{cm}^2$ 

**6.** 20.4375 cm<sup>2</sup>; 686.0625 cm<sup>2</sup>

7. 88.44 cm<sup>2</sup>

(i) 19.625 m<sup>2</sup>

(ii) 58.875 cm<sup>2</sup> **9.** (i) 285 mm

(ii)  $\frac{385}{4} \text{ mm}^2$ 

10.  $\frac{22275}{28}$  cm<sup>2</sup>

11.  $\frac{158125}{126}$  cm<sup>2</sup>

**12.** 189.97 km

**13.** ₹ 162.68

**14.** D

# **EXERCISE 12.1**

1. 160 cm<sup>2</sup>

2. 572 cm<sup>2</sup>

3. 214.5 cm<sup>2</sup>

4. Greatest diameter = 7 cm, surface area = 332.5 cm<sup>2</sup>

5.  $\frac{1}{4}l^2(\pi + 24)$ 

6. 220 mm<sup>2</sup>

7. 44 m<sup>2</sup>, ₹ 22000

8. 18 cm<sup>2</sup>

9. 374 cm<sup>2</sup>

# **EXERCISE 12.2**

1.  $\pi \text{ cm}^3$ 

2.  $66 \text{ cm}^3$ . Volume of the air inside the model = Volume of air inside (cone + cylinder + cone)  $= \left(\frac{1}{3}\pi r^2 h_1 + \pi r^2 h_2 + \frac{1}{3}\pi r^2 h_1\right), \text{ where } r \text{ is the radius of the cone and the cylinder, } h_1 \text{ is}$ the height (length) of the cone and  $h_2$  is the height (length) of the cylinder.

Required Volume =  $\frac{1}{3}\pi r^2 (h_1 + 3h_2 + h_1)$ .

**3.** 338 cm<sup>3</sup>

4. 523.53 cm<sup>3</sup>

**5.** 100

**6.** 892.26 kg

7. 1.131 m<sup>3</sup> (approx.)

**8.** Not correct. Correct answer is 346.51 cm<sup>3</sup>.

#### **EXERCISE 13.1**

1. 8.1 plants. We have used direct method because numerical values of  $x_i$  and  $f_i$  are small.

**2.** ₹545.20

**3.** f = 20

**4.** 75.9

**5.** 57.19

6. ₹ 211

7. 0.099 ppm

8. 12.48 days

**9.** 69.43 %

#### EXERCISE 13.2

- 1. Mode = 36.8 years, Mean = 35.37 years. Maximum number of patients admitted in the hospital are of the age 36.8 years (approx.), while on an average the age of a patient admitted to the hospital is 35.37 years.
- 2. 65.625 hours
- 3. Modal monthly expenditure = ₹ 1847.83, Mean monthly expenditure = ₹ 2662.5.
- 4. Mode: 30.6, Mean = 29.2. Most states/U.T. have a student teacher ratio of 30.6 and on an average, this ratio is 29.2.
- **5.** Mode = 4608.7 runs
- **6.** Mode = 44.7 cars

### **EXERCISE 13.3**

1. Median = 137 units, Mean = 137.05 units, Mode = 135.76 units. The three measures are approximately the same in this case.

**2.** x = 8, y = 7

3. Median age = 35.76 years

4. Median length = 146.75 mm

5. Median life = 3406.98 hours

**6.** Median = 8.05. Mean = 8.32. Modal size = 7.88

7. Median weight = 56.67 kg

#### **EXERCISE 14.1**

1. (i) 1 (ii) 0, impossible event

(iii) 1, sure or certain event

(iv) 1

(v) 0, 1

- 2. The experiments (iii) and (iv) have equally likely outcomes.
- 3. When we toss a coin, the outcomes head and tail are equally likely. So, the result of an individual coin toss is completely unpredictable.
- **4.** B

5, 0.95

**6.** (i) 0

7. 0.008

**8.** (i)  $\frac{3}{8}$  (ii)  $\frac{5}{8}$ 

**9.** (i)  $\frac{5}{17}$  (ii)  $\frac{8}{17}$  (iii)  $\frac{13}{17}$ 

**10.** (i)  $\frac{5}{9}$  (ii)  $\frac{17}{18}$ 

(ii) 1

260

11. 
$$\frac{5}{13}$$

**12.** (i) 
$$\frac{1}{8}$$
 (ii)  $\frac{1}{2}$  (iii)  $\frac{3}{4}$ 

(ii) 
$$\frac{1}{2}$$

(iii) 
$$\frac{3}{4}$$

**13.** (i) 
$$\frac{1}{2}$$

(ii) 
$$\frac{1}{2}$$

(ii) 
$$\frac{1}{2}$$
 (iii)  $\frac{1}{2}$ 

**14.** (i) 
$$\frac{1}{26}$$

(ii) 
$$\frac{3}{13}$$

(ii) 
$$\frac{3}{13}$$
 (iii)  $\frac{3}{26}$  (iv)  $\frac{1}{52}$  (v)  $\frac{1}{4}$ 

(iv) 
$$\frac{1}{52}$$

(v) 
$$\frac{1}{4}$$

(vi) 
$$\frac{1}{52}$$

**15.** (i) 
$$\frac{1}{5}$$

(ii) (a) 
$$\frac{1}{4}$$
 (b) 0

16. 
$$\frac{11}{12}$$

17. (i) 
$$\frac{1}{5}$$

(ii) 
$$\frac{15}{19}$$

17. (i) 
$$\frac{1}{5}$$
 (ii)  $\frac{15}{19}$  18. (i)  $\frac{9}{10}$  (ii)  $\frac{1}{10}$ 

(ii) 
$$\frac{1}{10}$$

(iii) 
$$\frac{1}{5}$$

**19.** (i) 
$$\frac{1}{3}$$
 (ii)  $\frac{1}{6}$  **20.**  $\frac{\pi}{24}$ 

(ii) 
$$\frac{1}{6}$$

20. 
$$\frac{\pi}{24}$$

**21.** (i) 
$$\frac{31}{36}$$

(ii) 
$$\frac{5}{26}$$

22.	(i
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Sum on 2 dice	2	3	4	5	6	7	8	9	10	11	12
Probability	1/36	$\frac{2}{36}$	$\frac{3}{36}$	$\frac{4}{36}$	<u>5</u> 36	$\frac{6}{36}$	5/36	4 36	$\frac{3}{36}$	$\frac{2}{36}$	1 36

- (ii) No. The eleven sums are not equally likely.
- $\frac{3}{4}$ ; Possible outcomes are: HHH, TTT, HHT, HTH, HTT, THH, THT, TTH. Here, THH means tail in the first toss, head on the second toss and head on the third toss and so on.
- 24.
- 25. (i) Incorrect. We can classify the outcomes like this but they are not then 'equally likely'. Reason is that 'one of each' can result in two ways — from a head on first coin and tail on the second coin or from a tail on the first coin and head on the second coin. This makes it twicely as likely as two heads (or two tails).
  - (ii) Correct. The two outcomes considered in the question are equally likely.

#### **EXERCISE A1.1**

1. (i) Ambiguous (ii) True (iii) True (iv) Ambiguous

- (v) Ambiguous
- 2. (i) True (ii) True (iii) False (iv) True (v) True
- 3. Only (ii) is true.
- **4.** (i) If a > 0 and  $a^2 > b^2$ , then a > b.
  - (ii) If  $xy \ge 0$  and  $x^2 = y^2$ , then x = y.
  - (iii) If  $(x + y)^2 = x^2 + y^2$  and  $y \ne 0$ , then x = 0.
  - (iv) The diagonals of a parallelogram bisect each other.

#### **EXERCISE A1.2**

- **1.** A is mortal **2.** *ab* is rational
- 3. Decimal expansion of  $\sqrt{17}$  is non-terminating non-recurring.
- **4.** y = 7 **5.**  $\angle A = 100^{\circ}, \angle C = 100^{\circ}, \angle D = 180^{\circ}$
- **6.** PQRS is a rectangle.
- 7. Yes, because of the premise. No, because  $\sqrt{3721} = 61$  which is not irrational. Since the premise was wrong, the conclusion is false.

# **EXERCISE A1.3**

1. Take two consecutive odd numbers as 2n + 1 and 2n + 3 for some integer n.

#### **EXERCISE A1.4**

- **1.** (i) Man is not mortal.
  - (ii) Line l is not parallel to line m.
  - (iii) The chapter does not have many exercises.
  - (iv) Not all integers are rational numbers.
  - (v) All prime numbers are not odd.
  - (vi) Some students are lazy.
  - (vii) All cats are black.
  - (viii) There is at least one real number x, such that  $\sqrt{x} = -1$ .

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- (ix) 2 does not divide the positive integer a.
- (x) Integers a and b are not coprime.
- **2.** (i) Yes
- (ii) No
- (iii) No
- (iv) No
- (v) Yes

#### **EXERCISE A1.5**

- **1.** (i) If Sharan sweats a lot, then it is hot in Tokyo.
  - (ii) If Shalini's stomach grumbles, then she is hungry.
  - (iii) If Jaswant can get a degree, then she has a scholarship.
  - (iv) If a plant is alive, then it has flowers.
  - (v) If an animal has a tail, then it is a cat.
- 2. (i) If the base angles of triangle ABC are equal, then it is isosceles. True.
  - (ii) If the square of an integer is odd, then the integer is odd. True.
  - (iii) If x = 1, then  $x^2 = 1$ . True.
  - (iv) If AC and BD bisect each other, then ABCD is a parallelogram. True.
  - (v) If a + (b + c) = (a + b) + c, then a, b and c are whole numbers. False.
  - (vi) If x + y is an even number, then x and y are odd. False.
  - (vii) If a parallelogram is a rectangle, its vertices lie on a circle. True.

#### **EXERCISE A1.6**

- **1.** Suppose to the contrary  $b \le d$ .
- 3. See Example 10 of Chapter 1.
- **6.** See Theorem 5.1 of Class IX Mathematics Textbook.

# **EXERCISE A2.2**

- 1. (i)  $\frac{1}{5}$  (ii) 160
- 2. Take 1 cm<sup>2</sup> area and count the number of dots in it. Total number of trees will be the product of this number and the area (in cm<sup>2</sup>).
- **3.** Rate of interest in instalment scheme is 17.74 %, which is less than 18 %.

#### **EXERCISE A2.3**

1. Students find their own answers.